

Because there are two different rules for $g(x)$ in different “pieces” of the domain, g is called a **piecewise function** of x .

PROPERTY: Absolute Value Transformations

The transformation $g(x) = |f(x)|$

- Reflects f across the x -axis if $f(x)$ is negative
- Leaves f unchanged if $f(x)$ is nonnegative

The transformation $g(x) = f(|x|)$

- Leaves f unchanged for nonnegative values of x
- Reflects the part of the graph for positive values of x to the corresponding negative values of x
- Eliminates the part of f for negative values of x

Even Functions and Odd Functions

Figure 1-6e shows the graph of $f(x) = -x^4 + 5x^2 - 1$, a polynomial function with only even exponents. (The number 1 equals $1x^0$, which has an even exponent.)

Figure 1-6f shows the graph of $f(x) = -x^3 + 6x$, a polynomial function with only odd exponents. What symmetries do you observe?

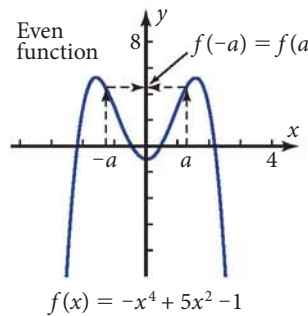


Figure 1-6e

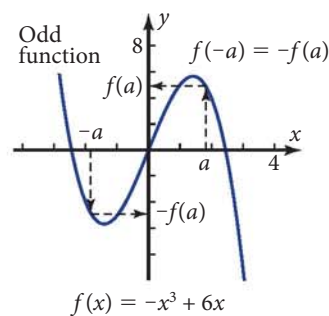


Figure 1-6f

Reflecting the graph of the even function $f(x) = -x^4 + 5x^2 - 1$ horizontally across the y -axis leaves the graph unchanged. You can see this algebraically given the property of powers with even exponents.

$$f(-x) = -(-x)^4 + 5(-x)^2 - 1 \quad \text{Substitute } -x \text{ for } x.$$

$$f(-x) = -x^4 + 5x^2 - 1 \quad \text{Negative number raised to an even power.}$$

$$f(-x) = f(x)$$

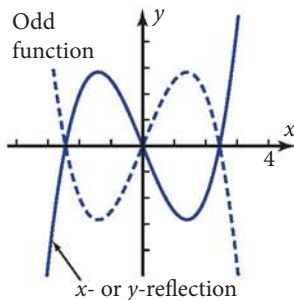


Figure 1-6g

Figure 1-6g shows that reflecting the graph of the odd function $f(x) = -x^3 + 6x$ horizontally across the y -axis has the same effect as reflecting it vertically across the x -axis. Algebraically,

$$f(-x) = -(-x)^3 + 6(-x) \quad \text{Substitute } -x \text{ for } x.$$

$$f(-x) = x^3 - 6x \quad \text{Negative number raised to an odd power.}$$

$$f(-x) = -f(x)$$